S.P. 2-K

For $\mathbf{F}(\mathbf{r}) = yz^2 \hat{\mathbf{a}}_x + xz^2 \hat{\mathbf{a}}_y + 2xyz \hat{\mathbf{a}}_z$, find the value of $\int_{P_1}^{P_2} \mathbf{F} \cdot d\ell$ where $P_1 = (0,0,0)$, $P_2 = (1,1,1)$ along

- a) A straight path from P_1 to P_2
- b) The path $y = x^2$ and $z = \sqrt{x}$ from P_1 to P_2
- c) Repeat a) and b) by noticing that the vector field $\mathbf{F}(\mathbf{r})$ can be expressed as the gradient of some scalar field $f(\mathbf{r})$.